

## The solid state & surface chemistry

### SUBJECTIVE PROBLEMS:

#### Q 1.

The density of mercury is 13.6 g/ml. Calculate approximately the diameter of an atom of mercury assuming that each atom is occupying a cube of edge length equal to the diameter of the mercury atom. (IIT JEE 1983 – 3 Marks)

#### Q 2.

Sodium metal crystallizes in body centred cubic lattice with the cell edge,  $a = 4.29 \text{ \AA}$ . What is the radius of sodium atom? (IIT JEE 1994 – 2 Marks)

#### Q 3.

A metallic element crystallizes into a lattice containing a sequence of layers of ABABAB..... Any packing of spheres leaves out voids in the lattice. What percentage by volume of this lattice is empty space? (IIT JEE 1996 – 3 Marks)

#### Q 4.

A unit cell of sodium chloride has four formula units. The edge length of the unit cell is 0.564 nm. What is the density of sodium chloride? (IIT JEE 1997C – 2 Marks)

#### Q 5.

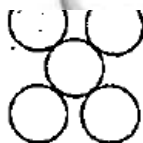
Chromium metal crystallizes with a body centered cubic lattice. The length of the unit cell edge is found to be 287 pm. Calculate the atomic radius. What would be the density of chromium in  $\text{g/cm}^3$ ? (IIT JEE 1997 – 3 Marks)

#### Q 6.

A metal crystallizes into cubic phases, face centered cubic (FCC), whose unit cell lengths are 3.5 and  $3.0 \text{ \AA}$ , respectively, Calculate the ratio of densities of FCC and BCC. (IIT JEE 1999 – 3 Marks)

#### Q 7.

The figures given below show the location of atoms in three crystallographic planes in a FCC lattice. Draw the unit cell for the corresponding structure and identify these planes in your diagram. (IIT JEE 2000 – 3 Marks)



**Q 8.**

You are given marbles of diameter 10 mm. They are to be placed such that their centres are lying in a square bound by four lines each of length 40 mm. What will be the arrangements of marbles in a plane so that maximum number of marbles can be placed inside the area? Sketch the diagram and derive expression for the number of molecules per unit area.

(IIT JEE 2000 – 2 Marks)

**Q 9.** 1 gm of charcoal adsorbs 100 ml 0.5 M  $\text{CH}_3\text{COOH}$  to form a monolayer, and thereby the molarity of  $\text{CH}_3\text{COOH}$  reduces to 0.49. Calculate the surface area of the charcoal adsorbed by each molecule of acetic acid. Surface area of charcoal =  $3.01 \times 10^2 \text{ m}^2/\text{gm}$ .

(IIT JEE 2003 – 2 Marks)

**Q 10.**

A compound AB has rock salt type structure. The formula weight of AB is  $6.023 Y \text{ amu}$ , and the closest A – B distance is  $Y^{1/3} \text{ nm}$ , where Y is an arbitrary number.

(IIT JEE 2004 – 2 Marks)

(a) Find the density of lattice

(b) If the density of lattice is found to be  $20 \text{ kg m}^{-3}$ , then predict the type of defect.

**Q 11.**

In face centered cubic (fcc) crystal lattice, edge length is 400 pm. Find the diameter of greatest sphere which can be fit into the interstitial void without distortion of lattice.

(IIT JEE 2005 – 2 Marks)

**Q 12.**

20% of surface sites are occupied by  $\text{N}_2$  molecules. The density of surface site is  $6.023 \times 10^{14} \text{ cm}^{-2}$  and total surface area is  $1000 \text{ cm}^2$ . The catalyst is heated to 300 K while  $\text{N}_2$  is completely desorbed into a pressure of 0.001 atm and volume of  $2.46 \text{ cm}^3$ . Find the number of active sites occupied by each  $\text{N}_2$  molecule.

(IIT JEE 2005 – 4 Marks)

**Q 13.**

The edge length of unit cell of a metal having molecular weight  $75 \text{ g/mol}$  is  $5 \text{ \AA}$  which crystallizes in cubic lattice. If the density is  $2 \text{ g/cc}$  then find the radius of metal atom ( $N_A = 6 \times 10^{23}$ ). Give the answer in pm.

(IIT JEE 2006 – 6 Marks)

## The solid state & surface chemistry-solutions

### SUBJECTIVE PROBLEMS:

#### Sol 1.

Avogadro's number =  $6.023 \times 10^{23}$

At. wt. of mercury(Hg) = 200

∴ In 1 g of Hg, the total number of atom  
=  $6.023 \times 10^{23} / 200 = 6.023 \times 10^{23} / 2 \times 10^2$   
=  $3.0115 \times 10^{21} = 3.012 \times 10^{21}$

∴ Density of Mercury (Hg) = 13.6 g/c.c.

∴ mass of  $3.012 \times 10^{21}$  atoms =  $1/3.012 \times 10^{21}$

Now volume of 1 atom of mercury (Hg)

=  $1/3.012 \times 10^{21} \times 13.6$  c.c. =  $10^3 \times 10 / 3012 \times 10^{21} \times 136$  c.c.  
=  $10^{-17} / 3012 \times 136$  c.c. =  $10^{-17} / 409632$  c.c. =  $1000000 \times 10^{-23} / 409632$  c.c.  
=  $2.44 \times 10^{-23}$  c.c.

Since each mercury atom occupies a cube of edge length equal to its diameter, therefore,

Diameter of one Hg atom =  $(2.44 \times 10^{-23})^{1/3}$  cm

=  $(24.4 \times 10^{-24})^{1/3}$  cm.

=  $2.905 \times 10^{-8}$  cm  $\equiv$  **2.91 Å**

#### Sol 2.

For bcc lattice, (radius),  $r = \sqrt{3}a/4$

Solution

∴  $r = \sqrt{3} \times 4.29 \text{ Å} / 4 = 1.73 \times 4.29 \text{ Å} / 4 = \mathbf{1.86 \text{ Å}}$

#### Sol 3.

For a hcp unit cell, there are 6 atoms per unit cell. If r is the radius of the metal atoms, volume occupied by the metallic

Atoms  $6 \times \frac{4}{3} \times \pi \times r^3 = 6 \times 1.33 \times \frac{22}{7} \times r^3 = 25.08 \times r^3$

Geometrically it has been shown that the base area of hcp unit cell

=  $6 \times \sqrt{3}/4 \times 4r^2$  and the height =  $4r \times \sqrt{2}/3$

∴ Volume of the unit cell

= Area \* height =  $6 \times \sqrt{3}/4 \times 4r^2 \times 4r \times \sqrt{\frac{2}{3}} = 33.94 r^3$

∴ Volume of the empty space of one unit cell

=  $33.94 r^3 - 25.08 r^3 = 8.86 r^3$

∴ Percentage void =  $8.816 r^3 / 33.94 r^3 \times 100 = \mathbf{26.1\%}$

**Sol 4.**

Density of NaCl

$$= n * \text{at. wt.}/\text{Av. No.} * a^3 = 4 * 58.5/6.023 * 10^{23} * (5.64 * 10^{-8})^3$$

$$= 2.16 \text{ g/cm}^3$$

**Sol 5.**For bcc lattice,  $r = \sqrt{3} * a/4 = \sqrt{3}/4 * 287 = 124.27 \text{ pm}$ Now Density =  $n * \text{at. wt.}/V * \text{Av. No.} = n * \text{at. wt.}/a^3 * \text{Av. No.}$ N = 2 for bcc;  $a = 287 * 10^{-10} \text{ cm}$ 

$$\therefore \text{Density} = 2 * 51.99/(287 * 10^{-10})^3 * 6.023 * 10^{23} = 7.30 \text{ g/ml}$$

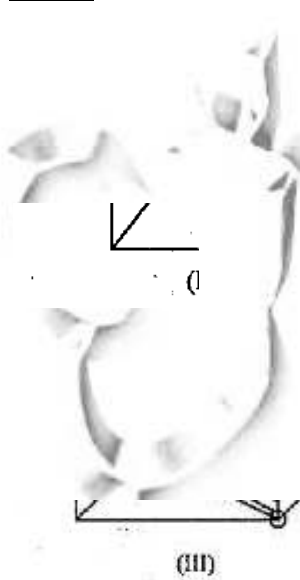
**Sol 6.**Density in fcc =  $n_1 * \text{at. wt.}/V_1 * \text{No.}$ Density in bcc =  $n_2 * \text{at. wt.}/V_2 * \text{No.}$ fcc unit cell length =  $3.5 \text{ \AA}$ bcc unit cell length =  $3.0 \text{ \AA}$ Density in fcc =  $n_1 * \text{at. wt.}/V_1 * \text{Av. No.}$ Density in bcc =  $n_2 * \text{at. wt.}/V_2 * \text{Av. No.}$ 

$$\therefore D_{\text{fcc}}/D_{\text{bcc}} = n_1/n_2 * V_2/V_1$$

$$n_1 \text{ for fcc} = 4; \text{ Also } V_1 = a^3 = (3.5 * 10^{-8})^3$$

$$n_2 \text{ for bcc} = 2; \text{ Also } V_2 = a^3 = (3.0 * 10^{-8})^3$$

$$\therefore D_{\text{fcc}}/D_{\text{bcc}} = 4 * (3.0 * 10^{-8})^3 / 2 * (3.5 * 10^{-8})^3 = 1.259$$

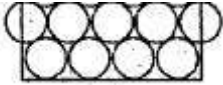
**Sol 7.**

### Sol 8.

The area of square =  $4 * 4 = 16 \text{ cm}^2$

Again to have the maximum number of spheres the packing must be hcp.

Maximum number of spheres =  $14 + 8 = 14 + 4 = 18$   
full half



Area =  $16 \text{ cm}^2$

$\therefore$  Number of spheres  $\text{cm}^2 = 18/16$   
 $= 1.126$

### Sol 9.

Number of moles of acetic in 100 ml before adding charcoal = 0.05

Number of moles of acetic acid in 100 ml after adding charcoal = 0.049

Number of moles of acetic acid adsorbed on the surface of charcoal = 0.001

Number of molecules of acetic acid adsorbed on the surface of charcoal =  $0.001 * 6.02 * 10^{23} = 6.02 * 10^{20}$

Surface area of charcoal =  $3.01 * 10^2 \text{ m}^2$  (given)

Area occupied by single acetic acid molecule on the surface of charcoal  $3.01 * 10^2 / 6.02 * 10^{20} = 5 * 10^{-19} \text{ m}^2$

### Sol 10.

(a) Density of AB =  $Z * M / N_0 * a^3$

Here, Z = 4 (for fcc), M = 6.023 Y,

A =  $2 Y^{1/3} \text{ nm} = 2 Y^{1/3} * 10^{-9} \text{ m}$

Thus,

Density =  $4 * 6.023 / 6.023 * 10^{23} * (2 Y^{1/3} * 10^{-9})^3$   
 $= 5.0 \text{ kg m}^{-3}$

(b) Since the observed density ( $20 \text{ kg m}^{-3}$ ) of AB is higher than the calculated ( $5 \text{ kg m}^{-3}$ ), the compound must have metal excess **defect**. Non-stocheometric defect.

### Sol 11.

For an octahedral void  $a = 2 (r + R)$  In fcc lattice the largest void present is octahedral void. If the radius of void sphere is R and of lattice sphere is r. Then,

$r = \sqrt{2} * 400 / 5 = 141.12 \text{ pm}$  (a = 400 pm)

applying condition for octahedral void,  $2 (r + R) = a$

$\therefore 2 R = a - 2r = 400 - 2 * 141.12 \therefore$  Diameter of greatest sphere = **117.16 pm**

**Sol 12.**

$$P_{N_2} = 0.001 \text{ atm}, T = 300 \text{ K}, V = 2.46 \text{ cm}^3$$

∴ Number of  $N_2$  molecules

$$= PV/RT * N_{AV} = 0.001 * 2.46 * 10^{-3} / 0.0821 * 300 * 6.023 * 10^{23}$$
$$= 6.016 * 10^{16}$$

Now total number of surface sites

$$= \text{Density} * \text{Total surface area}$$

$$= 6.023 * 10^{14} * 1000 = 6.023 * 10^{17}$$

$$\text{Sites occupied by } N_2 \text{ molecules} = 20/100 * 6.023 * 10^{17} = 12.04 * 10^{16}$$

∴ No. of sites occupied by each  $N_2$  molecule

$$= 12.04 * 10^{16} / 6.016 * 10^{16} = 2$$

**Sol 13.**

For bcc ;  $r = \sqrt{3}/2 a$ ;

$$d = n * M / N_{AV} * a^3 \text{ or } n = d * N_{AV} * a^3 / M$$

$$\Rightarrow n = 2 * 6 * 10^{23} (5 * 10^{-8})^3 / 75 = 2$$

Therefore Metal crystallizes in BCC structure and for a BCC lattice  $\sqrt{3}a = 4r$

$$r = \sqrt{3}/4 a = \sqrt{3} * 5/4 = 2.165 \text{ \AA} = 216.5 \text{ pm}$$

so the required answer is **217 pm**.