

- Ampere's circuital law  $\rightarrow$  The line integral of the magnetic field around a closed loop is  $\mu_0$  times the current threading the surface bound by the closed loop.

$$\oint \vec{B} \cdot d\vec{l} = \mu_0 I$$

- Maxwell found an inconsistency in Ampere's law, and suggested the existence of an additional current, called displacement current, to remove this inconsistency. This displacement current is due to a time-varying electric field, and is given by

$$i_d = \epsilon_0 \frac{d\phi_E}{dt}$$

- Maxwell's equations:

$$\text{First equation} \rightarrow \oint \vec{E} \cdot d\vec{s} = \frac{q}{\epsilon_0}$$

$$\text{Second equation} \rightarrow \oint \vec{B} \cdot d\vec{s} = 0$$

$$\text{Third equation} \rightarrow \oint \vec{E} \cdot d\vec{l} = -\frac{d\phi_B}{dt}$$

$$\text{Fourth equation} \rightarrow \oint \vec{B} \cdot d\vec{l} = \mu_0 i_c + \mu_0 \epsilon_0 \frac{d\phi_E}{dt}$$

- The speed of electromagnetic waves is given by

$$C = \frac{1}{\sqrt{\mu_0 \epsilon_0}},$$

Where,

$\mu_0 \rightarrow$  Permeability of free space

$\epsilon_0 \rightarrow$  Permittivity of free space

In material medium, the speed of light is given by

$$v = \frac{1}{\sqrt{\mu \epsilon}}$$

Where,  $\mu$  is the permeability of the medium and  $\epsilon$  its permittivity

- The rate of transfer of electromagnetic energy per unit area is represented by a quantity called Poynting vector  $\vec{S}$ . The direction of  $\vec{S}$  at any point gives the direction of energy transport at that point. Its SI unit is  $\text{Wm}^{-2}$ .

$$\vec{S} = \frac{1}{\mu_0} \vec{E} \times \vec{B}$$

- An electromagnetic wave carries linear momentum with it. If a portion of an electromagnetic wave has energy  $U$ , then the linear momentum carried by this portion of the wave is  $p = \frac{U}{c}$ .

- Intensity of electromagnetic wave is

$$I = \frac{1}{2} \epsilon_0 E_0^2 c$$

- Different electromagnetic waves:

-	Type	Wavelength range
(a)	Radio waves	$>0.1$ m
(b)	Microwave	0.1 m to 1 mm
(c)	Infra-red	1 mm to 700 nm
(d)	Visible light	700 nm to 400 nm
(e)	Ultra-violet	400 nm to 1 nm
(f)	X-rays	1 nm to $10^{-3}$ nm
(g)	Gamma rays	$<10^{-3}$ nm

