## 2.1 Line Integral of Electric Field

If a unit positive charge is displaced by dl in an electric field of intensity E , work done is given by

Line integration of this equation gives the work done in displacing a unit positive charge from P to Q as

$$W = \int_{P}^{Q} \vec{E} dI$$

This work depends only on the initial and final positions of the uniteral arge and not on the path followed by it. Hence, work done in moving a charge story a closed path is equal to zero. Thus electric field like gravitational field is a conservative field.

#### 2.2 Electrostatic Potential

The work done by the electric field in moving with positive electric charge from an arbitrarily selected reference point  $\theta$ , which may be incide or outside the field, to point P is given by

$$W_{P} = \int_{0}^{P} \frac{d}{E} dI$$

For the selected reference point, the value of Wp depends only on the position of point P and not on the path followed in going from reference point to point P.

Let  $\theta$  be at infinity. The electric field at infinite distance due to finite charge distribution will be zero. The electric field due to an infinitely long charged plane at infinite distance will not be zero. However, in plantice, one cannot have such a charge distribution.

The work down in a direction, opposing the electric field in bringing a unit positive charge from an intinity position to any point in the electric field is called the static electric potential (V) at that page.

Its sign baken as negative as the work done is in a direction opposite to the electric field.

Thus, work done in bringing a unit positive charge from infinity to points P and Q will be

$$V(P) = + \int_{\infty}^{P} \underbrace{E \cdot dI} \quad \text{and} \quad V(Q) = + \int_{\infty}^{Q} \underbrace{E \cdot dI}$$

$$V(Q) - V(P) = + \int_{\infty}^{Q} \underbrace{E \cdot dI} + \int_{\infty}^{P} \underbrace{E \cdot dI} = \int_{\infty}^{P} \underbrace{E \cdot dI} + \int_{Q}^{\infty} \underbrace{E \cdot dI}$$

$$= + \int_{P}^{Q} \underbrace{E \cdot dI}$$

This equation gives the electric potential of point Q with respect to point P. Its unit is volt (joule/coulomb) denoted by V and its dimensional formula is  $M^{1}L^{2}T^{-3}A^{-1}$ .

## 2.3 Electric Potential Energy and Potential Difference

A stationary electric charge at infinity has no energy (kinetic or potential) associated with it. If a unit positive charge is brought from infinity to an arbitrary point P in the electric field such that it has no velocity at that point then, the field being conservative, work done on it is stored with it in the form of potential energy and is called the electric potential of the point P and is given by

$$V(P) = -\int_{\infty}^{P} \vec{E} \cdot \vec{di}$$

If the electric charge is of magnitude q instead of unity, then the work done is called the potential energy of the charge q at point P and is given by

$$U(P) = qV(P) = \cdot \int_{QC}^{P} q \stackrel{\rightarrow}{E} \stackrel{\rightarrow}{\Box} di$$

The original electric field or the arrangement of makes in the field should remain unaffected by bringing the electric charge q or the unit charge to me an infinite distance to the point in the electric field.

Generally, one needs to calculate the potential difference or the difference in potential energy of charge q when it is moved from P to Q which is given by

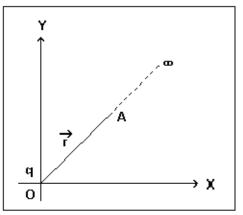
It should be noted that this Diential energy or the potential energy change is associated not only with the charge q at the so with the entire charge distribution which gives rise to the electric field.

# 2.4 Electric Petential due to a Point Charge

The electic has at any point A having r as its position-vector due to a point charge q placed at the origin of the co-ordinate system is given by

$$= \frac{1}{4\pi \varepsilon_0} \frac{q}{r^2} r = \frac{kq}{r^2} r$$

The electric potential at point A as shown in the figure is given by



$$V(A) = -\int_{\infty}^{A} E \cdot dI$$

Moving in the radial direction from infinity to point A, di = dr r

## 2-ELECTROSTATIC POTENTIAL AND CAPACITANCE

Page 3

$$\therefore V(A) = -\int_{\infty}^{A} \left(\frac{kq}{r^2}\right) \mathbb{I}(dr^r) = -kq \int_{\infty}^{A} \frac{dr}{r^2} = -kq \left[-\frac{1}{r}\right]_{\infty}^{r} = \frac{kq}{r}$$

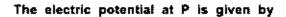
$$\therefore V(A) = V(r) = \frac{1}{4\pi \epsilon_0} \frac{q}{r}$$

The electric potential is positive if q is positive and negative if q is negative. Hence, for negative charge negative sign should be used for q in the above equation.

# 2.5 Electric Potential in the Field of an Electric Dipole

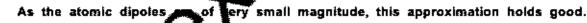
Let the two charges -q and +q be placed at A and B respectively with a distance 2a between them.

Let P be a point at a distance r from the centre of this dipole and making an angle  $\theta$  with its direction such that AP = r, and BP = r+



$$V(r) = \frac{1}{4\pi \epsilon_0} \frac{q}{r_+} \cdot \frac{1}{4\pi \epsilon_0} \frac{q}{r_-}$$
$$= \frac{q}{4\pi \epsilon_0} \left[ \frac{r_- - r_+}{r_- r_+} \right]$$

if r >> a, then  $r_+ \approx r_- \approx 1$  and  $r_- \cdot r_+ \approx 2a \cos \theta$ 



$$\therefore V(r) = \frac{q}{4\pi\epsilon_0} \left[ \frac{1}{r^2} \right] = \frac{1}{4\pi\epsilon_0} \frac{p\cos\theta}{r^2} \qquad (\because p = 2aq)$$

As p cos 
$$\vec{p}$$
  $\vec{r}$ ,  $\vec{v}$   $\vec{r}$   $\vec{r}$  =  $\frac{1}{4\pi \epsilon_0} \frac{\vec{p} \cdot \vec{r}}{r^2}$  (for  $|\vec{r}| >> 2a$ )

Note: If  $q \to \infty$  and  $a \to 0$  in p = 2qa, then the dipole is called a point dipole.

- (2) The above equation gives the exact value of the electric potential for a point dipole and an approximate value for a dipole system other than a point dipole.
- (3) For any point along the axis of the dipole,  $\theta=0$  or  $\pi$  and  $V=\pm\frac{1}{4\pi\,R_0}\,\frac{P}{r^2}$ .
- (4) For a point along the equator of the dipole,  $\theta = \pi/2$  and V = 0.
- (5) In the case of a dipole, the electric potential varies as 1/r<sup>2</sup> and not as 1/r as in the case of a point charge.

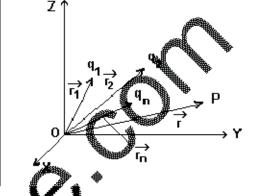
# 2.6 Electric Potentials due to Different Types of Charge Distributions

# 2.6 (a) Discrete Distribution of Charges:

The point electric charges  $q_1$ ,  $q_2$ , ...  $q_n$  have  $\xrightarrow{}$   $\xrightarrow{}$   $\xrightarrow{}$   $\xrightarrow{}$  respectively with respect to the origin.

The total electric potential at point P having position

vector r due to the entire charge distribution is equal to the algebraic sum of the electric potential due to each of the charges of the system and is given by



$$V = V_1 + V_2 + ... + V_8$$

$$= \frac{1}{4\pi \varepsilon_0} \left[ \frac{q_1}{\prod_{r=1}^{m} \frac{1}{r}} + \frac{q_2}{\prod_{r=1}^{m} \frac{1}{r}} + \dots + \frac{q_2}{\prod_{r=1}^{m} \frac{1}{r}} \right]$$

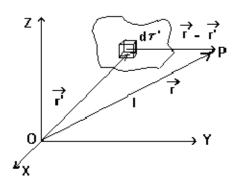
$$\therefore V(\vec{r}) = \sum_{i=1}^{n} \frac{kq_i}{|\vec{r} - \vec{r}_i|}$$

# 2.6 (b) Continuous Distribution of Charge:

Let  $\rho(r')$  = volume charge density for continuous charge distribution in some region.

dt' = small column element having position wearor, r'

The electric potential due to some volume element at some plant P having position vector,  $\vec{r}$ , is given by



$$= \frac{1}{4\pi \epsilon_0} \frac{\rho(r') dt'}{\frac{1}{1} \frac{1}{1} \frac{1}{1} \frac{1}{1} \frac{1}{1}}$$

integrating, we get the electric potential at the point P due to entire charge of the system as

$$V(\overrightarrow{r'}) = \frac{1}{4\pi \varepsilon_0} \int_{V} \frac{\rho(\overrightarrow{r'}) d\tau'}{|\overrightarrow{r} - \overrightarrow{r'}|}$$

For constant charge distribution,  $\rho(r') = \rho$  can be taken as constant.

## 2.6 (c) Uniformly Charged Spherical Shell:

For a spherical shell of radius R carrying charge q on its surface, the electric potential at a point outside the shell at a distance r from its centre can be calculated by treating the entire charge of the shell as if concentrated at its centre and is given by

$$V = \frac{1}{4\pi\epsilon_0} \frac{q}{r} \qquad \{r \ge R\}$$

The electric field inside the sphere is equal to zero. So the electric potential will be the same for all points inside the spherical shell and its value will be equal to the electric potential on the surface of the shell. Thus, the electric potential at the surface of the spherical shell and inside will be constant and is given by

$$V = \frac{1}{4\pi\epsilon_0} \frac{q}{R} \qquad (r \le R)$$

## 2.7 Equipotential Surfaces

If the electric potential at every point of any impoints y surface in an electric field is the same, then such a surface is called an equipment of surface.

As the electric potential at a distance r fue to spoint charge q is given by

$$V = \frac{1}{4\pi\epsilon_0} \frac{q}{\epsilon},$$

all concentric spherical surfaces the charge q at the centre are equipotential surfaces.

The electric intensity vector a any point is always perpendicular to the equipotential surface passing through that police. This can be proved as under.

Work done for small displacement di of a unit positive charge along the equipotential surface in a direction positive to the electric field

= . E an ential difference between the two points

0 (as the points are on equipotential surface)

(E) (dl) cos  $\theta$  = 0, where  $\theta$  is the angle between E and dl.

and di≠0, cosθ = 0

$$\therefore \cos \theta = \pi/2$$

which shows that E and di are perpendicular to each other. As di is tangential to the

surface of the sphere, E is perpendicular to the spherical surface which is equipotential. For uniform electric field, equipotential surfaces will be planes perpendicular to the electric field lines.

## 2.8 The Relation between Electric Field and Electric Potential

The electric potential difference between two close points P and Q is given by

$$\rightarrow$$
 ^  $\rightarrow$  ^ ^ \* If E = E<sub>x</sub> i and dl = dx i + dy j + dz k, then

$$dV = -(E_x i) \cdot (dx i + dy j + dz k) \qquad \therefore \quad dV = -E_x dx$$

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Similarly, if the electric field exists along the Y and Z directions, then

$$\frac{dV}{dy} = -E_y$$
 and  $\frac{dV}{dz} = -E_z$ 

If the electric field vector has all the three composite (x, y, z), then the relation between the electric field can be given as

$$\frac{\partial V}{\partial x} = -E_x$$
,  $\frac{\partial V}{\partial y} = -E_y$  and  $\frac{\partial V}{\partial z} = -E_z$ 

$$\vec{E} = -\left(\frac{\partial V}{\partial x} + \frac{\partial V}{\partial y} + \frac{\partial V}{\partial z}\right)$$

Here  $\frac{\partial V}{\partial x}$ ,  $\frac{\partial V}{\partial y}$  and  $\frac{\partial V}{\partial z}$  are partial derivatives of V(x,y,z) with respect to x,y and z respectively.

While taking the partial derivative of V(x,y,z) with respect to x, the remaining variables y and z are taken constant. Such a derivative of V is called its partial derivative with respect to x and is appoint  $\frac{\partial V}{\partial x}$ .

In general, the electric field exists along the r direction, then  $\frac{dV}{dr} = -E_r$ 

The electric field is a conservative field and the above equations can only be used for a conservative field.

## Potential Energy of a System of Charges

Work done in bringing electric charges from infinity to their respective positions in a system of charges gets stored in the form of electric potential energy of the system of charges.

The potential energy of a system of two charges q1 and q2 is given as

$$U_{12} = \frac{kq_1q_2}{\epsilon_{12}}$$

If a third charge  $q_3$  is introduced in the system, then the potential energy of the system of three charges will be

In general, if the system is made up of n electric charges,

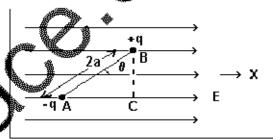
$$U = \sum_{\substack{i=1\\i < j}}^{n} U_{ij} = \sum_{\substack{i=1\\i < j}}^{n} \frac{kq_iq_j}{r_{ij}}$$

# 2.9 (a) Potential Energy of an Electric Dipole in a Uniform Electric Field

The potential energy of an electric dipole AB in a

uniform electric field (E) as shown in the figure is equal to the algebraic sum of the potential energy of the two charges of the dipole.

Taking the electric potential near the negative charge to be zero, the potential energy of the table will be equal to the potential energy of the tositive charge.



Let  $\Delta V$  be the change in electric poential as we move from A to B.

... the potential energy of this charge q at point B is

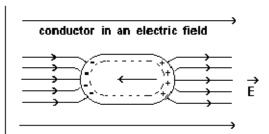
$$U = q \Delta V = -E(q \Delta r) c \Delta \theta = -Ep \cos \theta = -E \Box p$$

- (i) When the actric dipole is parallel to the field, E p = pE which means that the dipole is minimum potential energy (as it is more negative) which is also the equilibrium position of the dipole.
- = π, the dipole has maximum potential energy, pE, and is in an unsteady position.

When the electric dipole is perpendicular to the field ( $\theta = \pi/2$ ), the potential energy of the dipole is zero.

#### 2.10 Conductors and Electric Fields

When a conducting material is placed in a uniform electric field as shown in the figure, free electrons migrate in a direction opposite to the electric field and get deposited on one side of the metal surface while the positive charge gets deposited on the other side of the conductor. This produces an electric field inside the conductor and the migration of charges



stops when the internal electric field becomes equal to the external field.

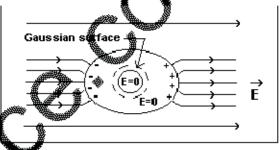
If we draw a Gaussian surface inside the conductor as shown in the figure, then since the electric field on it is zero, the net electric charge enclosed by it is also zero.

The important conclusions are:

- (1) Stationary electric charge distribution is induced on the surface of the conductor.
- (2) Both the electric field and the net electric charge inside the conductor are Len
- (3) At every point on the outer surface of the conductor, the electric field the perpendicular to the surface. This is so because the electric charge on the surface is stationary which means that no tangential force acts on it, thus proving that the lectric field on the surface has no tangential component.

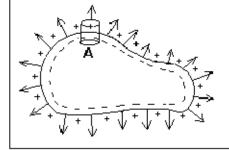
Consider another example of a hollow conductor placed in an external electric field.

Here also, the electric charges deposit on the outer surfaces and the electric field inside is zero as there is no charge inside. This phenomenon is called Electro-static Shielding. When a car is struck by lightning, the person sitting inside is saved from lightning as the car is hollow and acts like an electrostatic shield.



Electric field inside a charged conductor which is NOT in an electric field is also zero.

Consider a Gaussian surface close to the sociace of the conductor as shown by broken line in the houre. The line integration of the electric field along the Gaussian surface being zero, the net electric charge exclosed by it is also zero. This shows that in a charge conductor, the electric charge gets distributed on the ter surface of the conductor.



As the electric charge ware stationary, the direction of the electric field will be perpendicular to the surface of the conductor as shown the figure and its magnitude will be

$$\frac{\sigma}{\epsilon_0}$$

To explain its ensider a pillbox shaped Gaussian surface on the surface of the conductor as shown in the above figure.

The charge enclosed by the Gaussian surface = A or The total flux passing through this surface = A E

By Gauss's law, 
$$AE = A \frac{\sigma}{\epsilon_0}$$
  $\therefore E = \frac{\sigma}{\epsilon_0}$ 

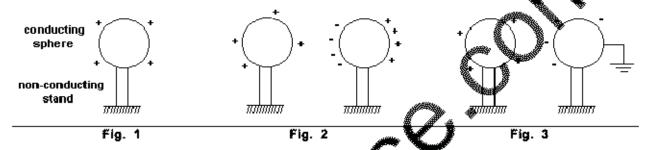
If G is not uniform along the surface, its proper value at the point should be used to calculate value of E at that point.

If a positive electric charge is placed in the cavity of the conductor as shown in the adjoining figure, it induces charges on the inner and outer surfaces of the conductor in such a way that the field will be zero in the interior portion of the conductor.



## 2.11 Capacitors and Capacitance

When positive electric charge on an isolated conducting sphere shown in figure 1 is gradually increased, electric potential on its surface and electric field in its vicinity increase. When the electric field becomes strong, it ionizes the surrounding air which causes charge on the sphere to leak and the charge on the sphere cannot be increased further. Turing this process, the ratio of charge (Q) and the electric potential (V) of the sphere remains constant. This ratio, Q/V, is called its capacitance (C).



To increase capacitance C of the sphere, another holds a conducting sphere is brought near it on which charge is induced as shown in figure 2. On earthing, the positive charge gets neutralized as shown in figure 3. The negative charge induced on the second sphere reduces the electric potential of the first sphere ther by increasing its charge storage capacity. The ratio Q / V of the charge on the first sphere and the potential difference between the two spheres is still constant and is call the opacitance C of the system. The value of C depends on the dimensions of the sphere, the distance between the two spheres and the medium between them.

The arrangement in which two good conductors of arbitrary shape and volume, are arranged close to one another, but separate from each other, is called a capacitor.

The conductors are known as plates of the capacitor. Positively charged conductor is called the positive plate and the negatively charged conductor the negative plate. Both the plates are equally charged, the charge on the positive plate is called the charge (Q) of the capacitor and taking the potential difference between the two plates as V, capacitance of the capacitor is Q = Q/V.

The S.I. (h) a capacitance is coulomb/volt which is also called farad (F) named after the great scientist michael Faraday. The smaller units of farad are microfarad ( $\mu F = 10^{-6} F$ ) and picefarad  $F = 10^{-12} F$ ).

## Parallel Plate Capacitor

tis type of capacitor is made by two metallic plates having identical area and kept parallel to each other. The distance (d) between the two plates is kept less as compared to the dimensions of the plates to minimize non-uniform electric field due to the irregular distribution of charges near the edges.

Let Q = electric charge on the capacitor  $\therefore \sigma = Q/A = \text{surface charge density}$ 

As d is very small, the plates can be considered as infinitely charged planes and the electric field between the plates can therefore be considered uniform.

2 εη

The electric fields,  $E_1$  and  $E_2$ , between the plates due to positively charged and negatively charged plates respectively are equal in magnitude and direction. The direction of both  $E_1$  and  $E_2$  is from the positively charged plate to the negatively charged plate.

The resultant electric field between the plates is, therefore,

$$E = E_1 + E_2 = \frac{\sigma}{2\epsilon_0} + \frac{\sigma}{2\epsilon_0} = \frac{\sigma}{\epsilon_0} = \frac{Q}{\epsilon_0 A} (\because \sigma = \frac{Q}{A})$$

Outside the plates,  $E_1$  and  $E_2$  being oppositely directed cancel each other resulting in zero electric field in this region.

The potential difference between the two plates is

$$V = E d = \frac{Q}{\epsilon_0 A} d$$
  $\therefore$  the capacitance of the capacitor  $C = \frac{d}{V} = \frac{\epsilon_0 A}{d}$ 

# 2.13 (a) Series Connection of Capacitors

The end to end connection of capacitors as sixwing in the figure is called the series connection capacitors.

Equal charge Q deposits on each calactur, but the p.d. between their plates is different depending on the value of its capacitance.

$$\frac{V}{Q} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_n}$$
 When all capacitors connected in series are replaced by a

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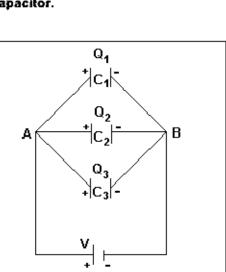
single capacity of capacitance C such that the charge deposited on it is Q with the same voltage supply the such a capacitor is called their equivalent capacitor.

$$\therefore \frac{\mathbf{v}}{\mathbf{c}} \qquad \therefore \frac{\mathbf{1}}{\mathbf{c}} = \frac{1}{\mathbf{c}_1} + \frac{1}{\mathbf{c}_2} + \dots + \frac{1}{\mathbf{c}_n}$$

raive of C is smaller than the smallest of  $C_1,\ C_2,\ \dots$ 

# 2.13 (b) Parallel Connection of Capacitors

The connection of capacitors in which positive plates of all capacitors are connected to a single point and negative plates to another single point in a circuit is called parallel connection of capacitors as shown in the figure. In such a connection, charge accumulated on each of the capacitors is different depending on the value of its capacitance, but the p.d. across all is the same.



Thus, total charge 
$$Q = Q_1 + Q_2 + Q_3 + ...$$
  
=  $\{C_1 + C_2 + C_3 + ....\} V$ 

When all capacitors connected in parallel are replaced by a single capacitor of capacitance C such that the charge deposited on it is Q with the same voltage supply, then such a capacitor is called their equivalent capacitor. Its value is

$$C = Q/V = C_1 + C_2 + C_3 + ...$$

## 2.14 Energy Stored in a Charged Capacitor

The work done in charging the capacitor gets stored in it in the form of penential energy.

The electric field on one plate due to charge Q and charge density  $\int_{\Omega} dt = \frac{\sigma}{2 E_0}$ 

The potential energy of one plate at a distance of from the other plate

UE = (electric p.d. between them) × (electric charge on the cond plate)

= 
$$\frac{\sigma d}{2\epsilon_0} \times Q$$
 (taking reference potential on the less plate as zero).

Putting 
$$\sigma = \frac{Q}{A}$$
,

$$U_{E} = \frac{Q}{A} \frac{d}{2\epsilon_{0}} D = \frac{Q^{2}}{2 D_{0} A/d} = \frac{Q}{C}$$

Putting Q = CV or C = Q/V, we get

$$U_E = \frac{Q^2}{2C} = \frac{1}{2}CV^2 = \frac{1}{2}Q$$

# Energy Stored in a Capacitor in terms of Energy Density of Electric Field

If A = area the plates of the capacitor d = apparation between the plates

then decree density of electric field in the capacitor

pp = emergy stored per unit volume

$$= \frac{U_E}{Ad} = \frac{1}{2} \frac{CV^2}{Ad} = \frac{1}{2} \frac{\epsilon_0 A}{d} \frac{V^2}{Ad} = \frac{1}{2} \epsilon_0 \left(\frac{V}{d}\right)^2$$
$$= \frac{1}{2} \epsilon_0 E^2 \left(\because \frac{V}{d} = E\right)$$

The above equation gives energy stored in a capacitor in terms of the energy stored in the electric field between the two plates. This is a general result which holds true for an electric field due to any charge distribution.

#### 2.15 Dielectric Substances and their Polarization

A non-conducting material is called a dielectric.

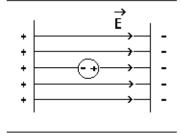
- The dielectric does not possess free electrons like a conducting material.
- Introduction of a dielectric between the two parallel plates of a capacitor considerably increases the capacitance of a capacitor.
- Dielectric materials are of two types: (1) Polar and (2) Non-polar.
- The atoms of a diefectric (like HCI, H<sub>2</sub>O) that have permanent dipole models is called a
  polar diefectric.
- The atoms of a dielectric (like H<sub>2</sub>, O<sub>2</sub>) that do not have permanent decir moment is called a non-polar dielectric.

# 2.15 (a) Non-polar Atoms (or Molecules) placed in a Unitor Electric Field:

The centres of the positive and the negative charges coincide in a non-polar dielectric atom or molecule. So it does not have permanent dipole moment

If such an atom or molecule is placed in a uniform electric

field (E), the centres of the positive and negative electric charges get separated due to electric force acting on them in opposite directions. This is known as polarization of the atom. If the electric field is not very strong, and the dipole moment,

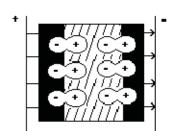


p, of the induced dipole is directly rop tional to E.

 $p = \alpha E$ , where constant  $\alpha = A B$  the atomic (or molecular) polarizability.

# 2.15 (b) Dielectric in 2 conscitor

A dielectric slab of pola niaterial is placed between the parallel plates of a capacitor shown in the figure. The torque due to the electric field acting on atomic dipoles aligns them in the direction of the electric field. In a solid dielectric material, its atoms perform cililatory motion, whereas in liquid or gas dielectric materials, they perform linear motion. The dipoles are in equilibrium and completely aligned as shown in the figure



when it electric potential energy, - p E, equals the thermal

the gy,  $\frac{1}{2}$  k T, due to absolute temperature T.

can be seen in the figure that the atomic dipoles line up such that the opposite polarity face each other canceling each other's effect. The net charge of the system is the charge of the capacitor plates. The dipole closer to the positive plate has negative charge lined up facing it and vice versa. These induced electrical charges are called bound charges.

The electric field between the capacitor plates is

$$E_f = \frac{\sigma_f}{\epsilon_0}$$
 (1) in the absence of the dielectric medium and is
$$E = \frac{\sigma_f - \sigma_b}{\epsilon_0}$$
 (2) in the presence of the dielectric slab.

$$E = \frac{\sigma_1 - \sigma_b}{\epsilon_0}$$
 (2) in the presence of the dielectric slab,

where  $\sigma_f$  is the free { controllable } surface charge density on the surface of the capacitor plates and  $\sigma_b$  is the bound surface charge density on the surface of the dielectric slab.  $\sigma_b$  is taken negative as the surface charges of the dielectric slab have opposite polarity as compared to the charges of the capacitor plates.

## Determining Ob

The dipole moment of the dielectric slab having surface area A and length L

$$P_t = \sigma_b A L \quad \triangle \quad \frac{P_t}{A L} = \frac{P_t}{V} = \sigma_b = P,$$

where  $P_1/V$  is the dipole moment of the dielectric slab per unit volume and P is called the intensity of polarization.

If the electric field is not very strong, the ratio of P and the electric field is a constant.

$$\therefore \chi_e = \frac{P}{E}$$

This ratio  $\chi_{\theta}$  is called the electric susceptibility of the dielectric material and its value depends on the dielectric material and its term grature.

$$\triangle P = \sigma_h = \chi_e E$$

$$\therefore E = \frac{\sigma_f}{\epsilon_0} - \frac{\rho}{\epsilon_0} = \frac{\sigma_f}{\epsilon_0} - \frac{\chi_{\rho}E}{\epsilon_0} \quad \text{[using equations (1) and (2)]}$$

$$\therefore E(e_0 + \chi_e) = \sigma_f = \Phi_p E_f$$

$$\therefore \quad \mathbf{E} = \left(\frac{\boldsymbol{\epsilon_0}}{\boldsymbol{\epsilon_0} + \boldsymbol{\chi_e}}\right)$$

Here,  $\mathcal{E}_0$  ,  $\chi_e$  =  $\mathcal{E}$  is called the permittivity of the medium and its value depends on the type of the discourage material and its temperature. Its unit is  $C^2 N^{-1} m^{-2}$ .

$$\therefore E_f = \frac{E_f}{E_{\xi_0}} = \frac{E_f}{E_r} = \frac{E_f}{K}$$

the relative permittivity  $\epsilon_r$  and is also called dielectric constant K.

This shows that when a dielectric material having dielectric constant K is placed as a medium between the capacitor plates, the electric field is reduced by a factor of K and the capacitance of the capacitor becomes

$$C_{i} = \frac{q}{\epsilon A} = \frac{\epsilon^{0} K A}{q} = K C$$

Thus when a dielectric medium having dielectric constant K is introduced in a capacitor, the value of its capacitance increases to K times the original capacitance.

From equation (2), we have  $\mathcal{E}_0 \to \mathcal{P} = \sigma_f \quad (\because \sigma_b = \mathcal{P})$ 

Here, E and P are electric and polarization fields respectively which are both vector quantities.

## 2.16 Van-de-Graf Generator

The principle of this machine is as under.

A conducting sphere having charge q and radius r is kept centrally inside a conducting shell having charge Q and radius R (r < R).

The electric potential on the spherical shell of radius on the surface of the sphere of radius r are respectively

$$V_R = \frac{kQ}{R} + \frac{kq}{R}$$
 and  $V_r = \frac{kQ}{R} + \frac{kq}{g_k}$ 

Hence, the potential difference between the surjects of the two spheres is

$$V_r - V_R = \frac{kQ}{R} + \frac{kq}{r} - \frac{kQ}{R} - \frac{kq}{R} = \left(\frac{1}{r} - \frac{1}{R}\right)$$

The above equation shows that the malier sphere is at a higher potential as compared to the large spherical shell. So if the two are connected through a conductor, then the electric charge will flow from the electric sphere to the larger spherical shell. So if charge is transferred continuously to the smaller sphere in some way, then it will accumulate on the larger shell thereby increasing its electric potential to a very large value.

Van-de-Graf used this principle to construct a generator known as Van-de-Graf generator to generate several pillion volts of electric potential.

As shown in the injure, a non-conducting belt is driven across to pulleys. The lower pulley is connected to a motor and the upper one is sufficiently a spherical shell. Positive electric charge transferred to the belt near the lower rull y using a discharge tube and a brush with him, edges. The electric charge moves to the deper pulley and is deposited on the outer shell with a metallic brush. Thus electric potential of the order of 6 to 8 million volts is generated on the outer shell.

The highly intense electric field produced in this device can accelerate electric charges which can be used to study the composition of matter at the microscopic level.

