

(1) If the cube roots of unity are  $1, \omega, \omega^2$ , then the roots of the equation  $(x - 1)^3 + 8 = 0$  are

- (a)  $-1, -1 + 2\omega, -1 - 2\omega^2$       (b)  $-1, -1, -1,$   
(c)  $-1, 1 - 2\omega, 1 - 2\omega^2$       (d)  $-1, 1 + 2\omega, 1 + 2\omega^2$       [ AIEEE 2005 ]

(2) If  $z_1$  and  $z_2$  are two non-zero complex numbers such that  $|z_1 + z_2| = |z_1| + |z_2|$ , then  $\arg z_1 - \arg z_2$  is equal to

- (a)  $\frac{\pi}{2}$       (b)  $-\pi$       (c)  $0$       (d)  $-\frac{\pi}{2}$       [ AIEEE 2005 ]

(3) If  $w = \frac{z}{z - \frac{1}{3}i}$  and  $|w| = 1$ , then  $z$  lies on

- (a) an ellipse      (b) a circle      (c) a straight line      (d) a parabola      [ AIEEE 2005 ]

(4) Let  $z, w$  be complex numbers such that  $\bar{z} + i\bar{w} = 0$  and  $\arg zw = \pi$ . Then  $\arg z$  equals

- (a)  $\frac{\pi}{4}$       (b)  $\frac{\pi}{2}$       (c)  $\frac{3\pi}{4}$       (d)  $\frac{5\pi}{4}$       [ AIEEE 2004 ]

(5) If  $z = x - iy$  and  $\frac{1}{z^3} = p + iq$ , then  $\frac{\left(\frac{x}{p} + \frac{y}{q}\right)}{p^2 + q^2}$  is equal to

- (a)  $1$       (b)  $-1$       (c)  $2$       (d)  $-2$       [ AIEEE 2004 ]

(6) If  $|z^2 - 1| = |z|^2 + 1$ , then  $z$  lies on

- (a) the real axis      (b) the imaginary axis  
(c) a circle      (d) an ellipse      [ AIEEE 2004 ]

(7) Let  $z_1$  and  $z_2$  be two roots of the equation  $z^2 + az + b = 0$ ,  $z$  being complex. Further assume that the origin,  $z_1$  and  $z_2$  form an equilateral triangle. Then

- (a)  $a^2 = b$       (b)  $a^2 = 2b$       (c)  $a^2 = 3b$       (d)  $a^2 = 4b$       [ AIEEE 2003 ]

(8) If  $z$  and  $w$  are two non-zero complex numbers such that  $|zw| = 1$  and  $\text{Arg}(z) - \text{Arg}(w) = \frac{\pi}{2}$ , then  $\bar{z}w$  is equal to

- (a) 1      (b) -1      (c)  $i$       (d)  $-i$

[ AIEEE 2003 ]

(9) If  $\left(\frac{1+i}{1-i}\right)^x = 1$ , then the value of smallest positive integer  $n$  is given by

- (a)  $x = 4n$       (b)  $x = 2n$       (c)  $x = 4n + 1$       (d)  $x = 2n + 1$

[ AIEEE 2003 ]

(10) If  $1, \omega, \omega^2$  are the cube roots of unity, then the value of  $\Delta = \begin{vmatrix} 1 & \omega & \omega^{2n} \\ \omega^n & \omega^{2n} & 1 \\ \omega^{2n} & 1 & \omega^n \end{vmatrix}$  is

- (a) 1      (b) 0      (c)  $\omega$       (d)  $\omega^2$

[ AIEEE 2003 ]

(11) If  $\frac{c+i}{c-i} = a+ib$ , where  $a, b, c$  are real, then the value of  $a^2 + b^2$  is

- (a) 1      (b)  $\frac{1}{c}$       (c)  $c^2$       (d)  $-c^2$

[ AIEEE 2002 ]

(12) If  $z = x + iy$ , then  $|3z - 1| = 3|z - 2|$  represents

- (a)  $x$ -axis      (b)  $y$ -axis      (c) a circle      (d) line parallel to  $y$ -axis

[ AIEEE 2002 ]

(13) If the cube roots of unity are  $1, \omega$  and  $\omega^2$ , then the value of  $\left(\frac{1+\omega}{\omega^2}\right)^3$  is

- (a) 1      (b)  $-1$       (c)  $\omega$       (d)  $\omega^2$

[ AIEEE 2002 ]

(14) If  $a = \cos \alpha + i \sin \alpha$  and  $b = \cos \beta + i \sin \beta$ , then the value of  $\frac{1}{2} \left( ab + \frac{1}{ab} \right)$  is

- (a)  $\sin(\alpha + \beta)$       (b)  $\cos(\alpha + \beta)$       (c)  $\sin(\alpha - \beta)$       (d)  $\cos(\alpha - \beta)$

[ AIEEE 2002 ]

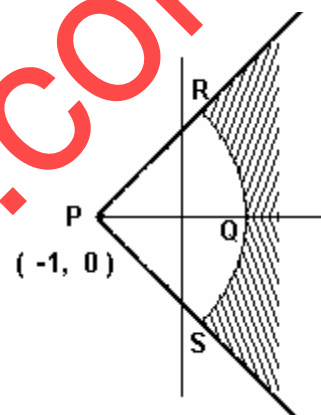
(15) If  $\alpha$  is cube root of unity, then for  $n \in \mathbb{N}$ , the value of  $\alpha^{3n+1} + \alpha^{3n+5}$  is

- (a) -1      (b) 0      (c) 1      (d) 3

[ AIEEE 2002 ]

(16) Four points  $P(-1, 0)$ ,  $Q(1, 0)$ ,  $R(\sqrt{2} - 1, \sqrt{2})$  and  $S(\sqrt{2} - 1, -\sqrt{2})$  are given on a complex plane, equation of the locus of the shaded region excluding the boundaries is given by

- (a)  $|z + 1| > 2$  and  $|\arg(z + 1)| < \frac{\pi}{4}$   
 (b)  $|z + 1| > 2$  and  $|\arg(z + 1)| < \frac{\pi}{2}$   
 (c)  $|z - 1| > 2$  and  $|\arg(z - 1)| < \frac{\pi}{4}$   
 (d)  $|z - 1| > 2$  and  $|\arg(z - 1)| < \frac{\pi}{2}$  [ IIT 2005 ]



(17) If  $\omega$  is cube root of unity ( $\omega \neq 1$ ), then the least value of  $n$  where  $n$  is a positive integer such that  $(1 + \omega^2)^n = (1 + \omega^4)^n$  is

- (a) 2      (b) 3      (c) 5      (d) 6

[ IIT 2004 ]

(18) The complex number  $z$  is such that  $|z| = 1$ ,  $z \neq -1$  and  $\omega = \frac{z-1}{z+1}$ , then real part of  $\omega$  is

- (a)  $\frac{1}{|z+1|^2}$       (b)  $\frac{-1}{|z+1|^2}$       (c)  $\frac{\sqrt{2}}{|z+1|^2}$       (d) 0 [ IIT 2003 ]

(19) Let  $\omega = -\frac{1}{2} + i\frac{\sqrt{3}}{2}$ . Then the value of the determinant  $\begin{vmatrix} 1 & 1 & 1 \\ 1 & -1 - \omega^2 & \omega^2 \\ 1 & \omega^2 & \omega^4 \end{vmatrix}$  is

- (a)  $3\omega$       (b)  $3\omega(\omega - 1)$       (c)  $3\omega^2$       (d)  $3\omega(1 - \omega)$  [ IIT 2002 ]

(20) For all complex numbers  $z_1, z_2$  satisfying  $|z_1| = 12$  and  $|z_2 - 3 - 4i| = 5$ , the minimum value of  $|z_1 - z_2|$  is

- (a) 0      (b) 2      (c) 7      (d) 17

[ IIT 2002 ]

(21) The complex numbers  $z_1$ ,  $z_2$  and  $z_3$  satisfying  $\frac{z_1 - z_3}{z_2 - z_3} = \frac{1 - i\sqrt{3}}{2}$  are the vertices of a triangle which is

- (a) of area zero      (b) right-angled isosceles  
(c) equilateral      (d) obtuse-angled isosceles

[ IIT 2001 ]

(22) If  $z_1$  and  $z_2$  be  $n$ th roots of unity which subtend a right angle at the origin, then  $n$  must be of the form

- (a)  $4k + 1$       (b)  $4k + 2$       (c)  $4k + 3$       (d)  $4k$

[ IIT 2001 ]

(23) If  $\arg(z) < 0$ , then  $\arg(-z) - \arg(z) =$

- (a)  $\pi$       (b)  $-\pi$       (c)  $-\frac{\pi}{2}$       (d)  $\frac{\pi}{2}$

[ IIT 2000 ]

(24) If  $z_1$ ,  $z_2$  and  $z_3$  are complex numbers such that

$$|z_1| = |z_2| = |z_3| = \left| \frac{1}{z_1} + \frac{1}{z_2} + \frac{1}{z_3} \right| = 1, \text{ then } |z_1 + z_2 + z_3| \text{ is}$$

- (a) 1      (b)  $< 1$       (c)  $> 3$       (d) 3

[ IIT 2000 ]

(25) If  $i = \sqrt{-1}$  then  $4 + 5 \left( -\frac{1}{2} + \frac{i\sqrt{3}}{2} \right)^{334} + 3 \left( -\frac{1}{2} + \frac{i\sqrt{3}}{2} \right)^{365}$  is equal to

- (a)  $1 - i\sqrt{3}$       (b)  $-1 + i\sqrt{3}$       (c)  $i\sqrt{3}$       (d)  $-i\sqrt{3}$

[ IIT 1999 ]

(26) If  $\omega$  is an imaginary cube root of unity, then  $(1 + \omega - \omega^2)^7$  equals

- (a)  $128\omega$       (b)  $-128\omega$       (c)  $128\omega^2$       (d)  $-128\omega^2$

[ IIT 1998 ]

(27) The value of the sum  $\sum_{n=1}^{13} (i^n + i^{n+1})$ , where  $i = \sqrt{-1}$ , equals

- (a)  $i$       (b)  $i - 1$       (c)  $-i$       (d) 0

[ IIT 1998 ]

(28) If  $\begin{vmatrix} 6i & -3i & 1 \\ 4 & 3i & -1 \\ 20 & 3 & i \end{vmatrix} = x + iy$ , then

- (a)  $x = 3, y = 1$       (b)  $x = 1, y = 3$   
(c)  $x = 0, y = 3$       (d)  $x = 0, y = 0$

[ IIT 1998 ]

(29) For positive integers  $n_1, n_2$ , the value of the expression  $(1+i)^{n_1} + (1+i^3)^{n_1} + (1+i^5)^{n_2} + (1+i^7)^{n_2}$ , where  $i = \sqrt{-1}$  is a real number if and only if

- (a)  $n_1 = n_2 + 1$     (b)  $n_1 = n_2 - 1$     (c)  $n_1 = n_2$     (d)  $n_1 > n_2 > 0$       [ IIT 1996 ]

(30) If  $\omega (\neq 1)$  is a cube root of unity and  $(1+\omega)^7 = A + B\omega$ , then A and B are respectively the numbers

- (a) 0, 1      (b) 1, 1      (c) 1, 0      (d) -1, 1      [ IIT 1995 ]

(31) If  $\omega (\neq 1)$  is a cube root of unity, then  $\begin{vmatrix} 1 & 1+i\omega^2 & \omega^2 \\ 1-i & -1 & \omega^2-1 \\ -i & i+\omega-1 & -1 \end{vmatrix}$  equals

- (a) 0      (b) 1      (c) i      (d)  $\omega$       [ IIT 1995 ]

(32) If  $z$  and  $\omega$  be two non-zero complex numbers such that  $|z| = |\omega|$  and  $\text{Arg } z + \text{Arg } \omega = \pi$ , then  $z$  equals

- (a)  $\omega$       (b)  $-\omega$       (c)  $\bar{\omega}$       (d)  $-\bar{\omega}$       [ IIT 1995 ]

(33) If  $z$  and  $w$  be two complex numbers such that  $|z| \leq 1, |w| \leq 1$  and  $|z+iw| = |z-iw| = 2$ , then  $z$  equals

- (a) 1 or i      (b) i or -i      (c) 1 or -1      (d) i or -1      [ IIT 1995 ]

(34) The complex numbers  $\sin x + i \cos 2x$  and  $\cos x - i \sin 2x$  are conjugate to each other for

- (a)  $x = n\pi$     (b)  $x = 0$     (c)  $x = (n+1/2)\pi$     (d) no value of  $x$       [ IIT 1988 ]

(35) If  $z_1$  and  $z_2$  are two non-zero complex numbers such that  $|z_1 + z_2| = |z_1| + |z_2|$ , then  $\arg z_1 - \arg z_2$  is equal to

- (a)  $-\pi$       (b)  $-\frac{\pi}{2}$       (c) 0      (d)  $\frac{\pi}{2}$       (e)  $\pi$       [ IIT 1987 ]

(36) The value of  $\sum_{k=1}^6 \left( \sin \frac{2\pi k}{7} - i \cos \frac{2\pi k}{7} \right)$  is

- (a) -1      (b) 0      (c) -i      (d) i      (e) none of these      [ IIT 1987 ]

(37) Let  $z_1$  and  $z_2$  be complex numbers such that  $z_1 \neq z_2$  and  $|z_1| = |z_2|$ . If  $z_1$  has positive real part and  $z_2$  has negative imaginary part, then  $\frac{z_1 + z_2}{z_1 - z_2}$  may be

- (a) zero      (b) real and positive      (c) real and negative  
(d) purely imaginary      (e) none of these      [ IIT 1986 ]

(38) If  $a, b, c$  and  $u, v, w$  are complex numbers representing the vertices of two triangles such that  $c = (1 - r)a + b$  and  $w = (1 - r)u + rv$ , where  $r$  is a complex number, then the two triangles

- (a) have the same area      (b) are similar  
(c) are congruent      (d) none of these      [ IIT 1985 ]

(39) If  $z_1 = a + ib$  and  $z_2 = c + id$  are complex numbers such that  $|z_1| = |z_2| = 1$  and  $\operatorname{Re}(z_1 \overline{z_2}) = 0$ , then the pair of complex numbers  $w_1 = a + ic$  and  $w_2 = b + id$  satisfies

- (a)  $|w_1| = 1$       (b)  $|w_2| = 1$   
(c)  $\operatorname{Re}(w_1 \overline{w_2}) = 0$       (d) none of these      [ IIT 1985 ]

(40) If  $z = x + iy$  and  $w = \frac{1 - iz}{z - i}$ , then  $|w| = 1$  implies that, in the complex plane,

- (a)  $z$  lies on the imaginary axis      (b)  $z$  lies on the real axis  
(c)  $z$  lies on the unit circle      (d) None of these      [ IIT 1983 ]

